

Comment on 15b)

i) As the problem is stated in the text, $f \circ g$ might not be defined on I . This is because some value $g(x)$ might be outside I , in which case $f(g(x))$ might not be defined.

So assume $\text{domain}(f) = \text{domain}(g) = I$ and that $\text{range}(g) \subseteq I$. Then $f \circ g$ will be defined on I .

ii) The chain rule, from calculus, might give you some insight about the problem. But you can't actually use the chain rule in any solution because we are not assuming f and g are differentiable.

iii) If you think the statement is false and are trying to construct a counterexample, then your counterexample should involve 2 specific functions f, g and a specific interval I . The domains and ranges should satisfy the condition given above, in i).