Here are the instructions from the exam:

## Part I

Some of the statements below are always correct the others are sometimes incorrect. Indicate which are which by marking

- **a** for statements that are **A** ways true
- **b** for statements that may **B** e false

Here are some statements that could have been used:

- If f(x, y) is a continuous function on the region R of all (x, y) with  $x^2 + y^2 < 1$  then f(x, y) must have a maximum at some point in that region.
- If you use the method of Lagrange multipliers to solve the problem of maximizing  $K^{1/2}L^{1/3} 2K 3L$  with the constraint 2K + 6L = 3 then the value of  $\lambda$ , the Lagrange multiplier, that you find is the partial elasticity of K with respect to L.
- If the function f(x, y) does not have a maximum in the region R then the function g(x, y) = 6 3f(x, y) does not have a minimum in R
- The point in the plane 2x + 3y + 4z = 6 that is closest to the origin is also the point that minimizes the function  $f(x, y, z) = x^2 + y^2 + z^2$  subject to the constraint 2x + 3y + 4z = 6.
- The Envelope Theorem gives a technique for testing if a critical point of a function is a local maximum.