

1. Which of the following are critical points of the function $f(x) = 1 - (x - 1)^{2/3}$?

A) 0

B) 1

C) $5/4$

D) $7/3$

E) $\sqrt{2}$

F) $\sqrt{3}$

G) π

H) 2π

I) 3π

J) None of the above

2. The continuous function $f(x) = x^3 - 12x^2 + 21x$ attains a maximum value on the closed interval $[0, 2]$. At which x does this occur?

A) 0

B) 1

C) $5/4$

D) $7/3$

E) $\sqrt{2}$

F) $\sqrt{3}$

G) π

H) 2π

I) 3π

J) None of the above

3. Find the maximum value taken on by $f(x) = \sin x \cos x$ on the interval $[0, \pi/2]$.

A) 0

B) $1/3$

C) $1/2$

D) $1/\sqrt{2}$

E) $1/\sqrt{3}$

F) $1/\pi$

G) $1/2\pi$

H) $\pi/3\sqrt{2}$

I) $\pi/2\sqrt{3}$

J) None of the above

4. Consider the function $f(x) = e^x - x$ on the interval $[-1, 1]$. Find a point c in the interval which satisfies the conclusion of the mean value theorem for this $f(x)$ and $[a, b]$. $c =$

A) 0

B) .0082

C) .0132

D) .1126

E) .1375

F) .1614

G) .1853

H) .2054

I) .2709

J) None of the above

5. The function $f(x) = 3x^5 - 5x^3$ is decreasing on an interval $[-1, a]$ and then is increasing on $[a, \infty)$. Find a .

A) 0

B) 1

C) $5/4$

D) $7/3$

E) $\sqrt{2}$

F) $\sqrt{3}$

G) π

H) 2π

I) 3π

J) None of the above

6. $f(x) = x^{5/3}$ changes concavity at only one point a . Find a .

A) 0

B) $1/3$

C) $1/2$

D) $1/\sqrt{2}$

E) $1/\sqrt{3}$

F) $1/\pi$

G) $1/2\pi$

H) $\pi/3\sqrt{2}$

I) $\pi/2\sqrt{3}$

J) None of the above

7. the function $f(x) = \frac{1}{x^2 + 1}$ has a single point of inflection in the interval $(0, \infty)$.

Find it.

A) 0

B) $1/3$

C) $1/2$

D) $1/\sqrt{2}$

E) $1/\sqrt{3}$

F) $1/\pi$

G) $1/2\pi$

H) $\pi/3\sqrt{2}$

I) $\pi/2\sqrt{3}$

J) None of the above

8. the function $f(x) = e^{-x^2}$ has a single point of inflection in the interval $(0, \infty)$. Find it.

A) 0

B) $1/3$

C) $1/2$

D) $1/\sqrt{2}$

E) $1/\sqrt{3}$

F) $1/\pi$

G) $1/2\pi$

H) $\pi/3\sqrt{2}$

I) $\pi/2\sqrt{3}$

J) None of the above

9. Find any points x at which the function $f(x) = \frac{x^2}{x^2 - 5x + 6}$ has a vertical asymptote.

A) 1

B) 2

C) 3

D) -2

E) -3

F) 2 and 3

G) 1 and 2

H) -1 and 3

I) -2 and -3

J) None of the above

10. Find any lines $y = b$ which are horizontal asymptotes of $f(x) = \frac{x^2}{x^2 - 5x + 6}$. $b =$

A) 0

B) 1

C) $5/4$

D) $7/3$

E) $\sqrt{2}$

F) $\sqrt{3}$

G) π

H) 2π

I) 3π

J) None of the above

11. Find the x – coordinate of the point on the curve $y = \sqrt{x}$ which is closest to the point $(1, 0)$.

A) 0

B) $1/3$

C) $1/2$

D) $1/\sqrt{2}$

E) $1/\sqrt{3}$

F) $1/\pi$

G) $1/2\pi$

H) $\pi/3\sqrt{2}$

I) $\pi/2\sqrt{3}$

J) None of the above

12. A box will be constructed from two kinds of sheet metal. The metal for the top and bottom, which are to be square, costs \$1 per m^2 . The metal for the sides costs \$2 per m^2 . To the nearest dollar, what is the material cost for the cheapest such box whose volume is 20 m^3 ?

- A) 16
- B) 43
- C) 70
- D) 124
- E) 467
- F) 1085
- G) 5238
- H) 11664
- I) 15893
- J) None of the above

13. What is the maximum possible area of a right triangle the length of whose legs add up to 2?

A) 0

B) $1/3$

C) $1/2$

D) $1/\sqrt{2}$

E) $1/\sqrt{3}$

F) $1/\pi$

G) $1/2\pi$

H) $\pi/3\sqrt{2}$

I) $\pi/2\sqrt{3}$

J) None of the above

14. According to U. S. Postal regulations, a rectangular box is “oversized” if the sum of its height and its girth (perimeter of the base) exceeds 108 inches. Find the maximum volume (in cubic inches) that a box can have if 1) it has a square base, and 2) it is *not* oversized.

A) 16

B) 43

C) 70

D) 124

E) 467

F) 1085

G) 5238

H) 11664

I) 15893

J) None of the above

15. Evaluate $\lim_{x \rightarrow 0^+} \left(\frac{1}{\sin x} - \frac{1}{x} \right)$.

A) 0

B) $1/3$

C) $1/2$

D) $1/\sqrt{2}$

E) $1/\sqrt{3}$

F) $1/\pi$

G) $1/2\pi$

H) $\pi/3\sqrt{2}$

I) $\pi/2\sqrt{3}$

J) None of the above

16. Find $\lim_{x \rightarrow 1} \frac{\tan^{-1} x - \pi/4}{\tan(\frac{\pi}{4} x) - 1}$.

A) 0

B) 1/3

C) 1/2

D) $1/\sqrt{2}$

E) $1/\sqrt{3}$

F) $1/\pi$

G) $1/2\pi$

H) $\pi/3\sqrt{2}$

I) $\pi/2\sqrt{3}$

J) None of the above

17. Suppose Newton's method is used to approximate a root of $x^4 + x^2 - 2x - 1 = 0$. The initial guess is $x_0 = 1$. Find the next approximation x_1 .

A) 0

B) 1

C) $5/4$

D) $7/3$

E) $\sqrt{2}$

F) $\sqrt{3}$

G) π

H) 2π

I) 3π

J) None of the above

18. Evaluate $\lim_{x \rightarrow \infty} \frac{3x^6 + 4x^2 - 7}{9x^6 + 12x^4 + 2x}$.

A) 0

B) $1/3$

C) $1/2$

D) $1/\sqrt{2}$

E) $1/\sqrt{3}$

F) $1/\pi$

G) $1/2\pi$

H) $\pi/3\sqrt{2}$

I) $\pi/2\sqrt{3}$

J) None of the above

19. Let $y(t)$ be the solution to the initial value problem $\frac{dy}{dt} = 5 - 2t^2$, $y(1) = \frac{20}{3}$.

Find $y(0)$.

A) 0

B) 1

C) $5/4$

D) $7/3$

E) $\sqrt{2}$

F) $\sqrt{3}$

G) π

H) 2π

I) 3π

J) None of the above

20. Let $y(x)$ be the solution of $\frac{dy}{dx} = \sec^2 3x$, $y\left(\frac{\pi}{4}\right) = 2$. Find $y(0)$.

A) 0

B) 1

C) $5/4$

D) $7/3$

E) $\sqrt{2}$

F) $\sqrt{3}$

G) π

H) 2π

I) 3π

J) None of the above