

13. An equation of the sphere with center  $(-3, 2, 5)$  and radius 4 is  $[x - (-3)]^2 + (y - 2)^2 + (z - 5)^2 = 4^2$  or  $(x + 3)^2 + (y - 2)^2 + (z - 5)^2 = 16$ . The intersection of this sphere with the  $yz$ -plane is the set of points on the sphere whose  $x$ -coordinate is 0. Putting  $x = 0$  into the equation, we have  $9 + (y - 2)^2 + (z - 5)^2 = 16$ ,  $x = 0$  or  $(y - 2)^2 + (z - 5)^2 = 7$ ,  $x = 0$ , which represents a circle in the  $yz$ -plane with center  $(0, 2, 5)$  and radius  $\sqrt{7}$ .
14. An equation of the sphere with center  $(2, -6, 4)$  and radius 5 is  $(x - 2)^2 + [y - (-6)]^2 + (z - 4)^2 = 5^2$  or  $(x - 2)^2 + (y + 6)^2 + (z - 4)^2 = 25$ . The intersection of this sphere with the  $xy$ -plane is the set of points on the sphere whose  $z$ -coordinate is 0. Putting  $z = 0$  into the equation, we have  $(x - 2)^2 + (y + 6)^2 = 9$ ,  $z = 0$  which represents a circle in the  $xy$ -plane with center  $(2, -6, 0)$  and radius 3. To find the intersection with the  $xz$ -plane, we set  $y = 0$ :  $(x - 2)^2 + (z - 4)^2 = -11$ . Since no points satisfy this equation, the sphere does not intersect the  $xz$ -plane. (Also note that the distance from the center of the sphere to the  $xz$ -plane is greater than the radius of the sphere.) To find the intersection with the  $yz$ -plane, we set  $x = 0$ :  $(y + 6)^2 + (z - 4)^2 = 21$ ,  $x = 0$ , a circle in the  $yz$ -plane with center  $(0, -6, 4)$  and radius  $\sqrt{21}$ .
15. The radius of the sphere is the distance between  $(4, 3, -1)$  and  $(3, 8, 1)$ :  $r = \sqrt{(3 - 4)^2 + (8 - 3)^2 + [1 - (-1)]^2} = \sqrt{30}$ . Thus, an equation of the sphere is  $(x - 3)^2 + (y - 8)^2 + (z - 1)^2 = 30$ .
19. Completing squares in the equation  $2x^2 - 8x + 2y^2 + 2z^2 + 24z = 1$  gives  $2(x^2 - 4x + 4) + 2y^2 + 2(z^2 + 12z + 36) = 1 + 8 + 72 \Rightarrow 2(x - 2)^2 + 2y^2 + 2(z + 6)^2 = 81 \Rightarrow (x - 2)^2 + y^2 + (z + 6)^2 = \frac{81}{2}$ , which we recognize as an equation of a sphere with center  $(2, 0, -6)$  and radius  $\sqrt{\frac{81}{2}} = 9/\sqrt{2}$ .
29. The inequality  $0 \leq z \leq 6$  represents all points on or between the horizontal planes  $z = 0$  (the  $xy$ -plane) and  $z = 6$ .
35. The inequalities  $1 \leq x^2 + y^2 + z^2 \leq 5$  are equivalent to  $1 \leq \sqrt{x^2 + y^2 + z^2} \leq \sqrt{5}$ , so the region consists of those points whose distance from the origin is at least 1 and at most  $\sqrt{5}$ . This is the set of all points on or between spheres with radii 1 and  $\sqrt{5}$  and centers  $(0, 0, 0)$ .
36. The equation  $x = z$  represents a plane perpendicular to the  $xz$ -plane and intersecting the  $xz$ -plane in the line  $x = z, y = 0$ .
45. We need to find a set of points  $\{P(x, y, z) \mid |AP| = |BP|\}$ . 
$$\sqrt{(x + 1)^2 + (y - 5)^2 + (z - 3)^2} = \sqrt{(x - 6)^2 + (y - 2)^2 + (z + 2)^2} \Rightarrow (x + 1)^2 + (y - 5)^2 + (z - 3)^2 = (x - 6)^2 + (y - 2)^2 + (z + 2)^2 \Rightarrow x^2 + 2x + 1 + y^2 - 10y + 25 + z^2 - 6z + 9 = x^2 - 12x + 36 + y^2 - 4y + 4 + z^2 + 4z + 4 \Rightarrow 14x - 6y - 10z = 9$$
 Thus the set of points is a plane perpendicular to the line segment joining  $A$  and  $B$  (since this plane must contain the perpendicular bisector of the line segment  $AB$ ).