

1.(1 pt) Find the particular solution of the differential equation

$$\frac{dy}{dx} = (x - 5)e^{-2y}$$

satisfying the initial condition $y(5) = \ln(5)$.

Answer: $y =$ _____

Your answer should be a function of x .

2.(1 pt) Find the particular solution of the differential equation

$$\frac{x^2}{y^2 - 6} \frac{dy}{dx} = \frac{1}{2y}$$

satisfying the initial condition $y(1) = \sqrt{7}$.

Answer: $y =$ _____

Your answer should be a function of x .

3.(1 pt) Find u from the differential equation and initial condition.

$$\frac{du}{dt} = e^{1.2t - 1.8u}, \quad u(0) = 3.6.$$

$u =$ _____

4.(1 pt) Solve the separable differential equation for u .

$$\frac{du}{dt} = e^{6u + 6t}$$

Use the following initial condition: $u(0) = 12$

$u =$ _____

5.(1 pt) Solve the separable differential equation for u .

$$\frac{du}{dt} = e^{2u + 8t}$$

Use the following initial condition: $u(0) = -13$

$u =$ _____

6.(1 pt) Solve the separable differential equation

$$10x - 6y\sqrt{x^2 + 1} \frac{dy}{dx} = 0$$

Subject to the initial condition: $y(0) = 2$

$y =$ _____

(function of x only)

7.(1 pt) Find $f(x)$ if $y = f(x)$ satisfies

$$\frac{dy}{dx} = 85yx^{16}$$

and the y intercept of the curve $y = f(x)$ is 2.

$f(x) =$ _____

8.(1 pt) Find an equation of the curve that satisfies.

$$\frac{dy}{dx} = 85yx^{16}$$

and whose y intercept is 6.

$y(x) =$ _____

(function of x)

9.(1 pt) Find the solution of the differential equation

$$3e^{5x} \frac{dy}{dx} = -25 \frac{x}{y^2}$$

which satisfies the initial condition $y(0) = 1$

$y =$ _____

10.(1 pt) Find a function y of x such that

$$9yy' = x \text{ and } y(9) = 8.$$

$y =$ _____ (function of x)

11.(1 pt) Solve the separable differential equation.

$$4yy' = x$$

Use the following initial condition: $y(4) = 7$

$x^2 =$ _____ (function of y)

12.(1 pt) Solve the differential equation

$$(y^3 x) \frac{dy}{dx} = 1 + x.$$

Use the initial condition $y(1) = 6$.

Express y^4 in terms of x .

$y^4 =$ _____

(function of x)

13.(1 pt) Solve the separable differential equation for.

$$\frac{dy}{dx} = \frac{1+x}{xy^6}; x > 0$$

Use the following initial condition: $y(1) = 5$

$y^7 =$ _____

(function of x)

14.(1 pt) Find the function $y = y(x)$ (for $x > 0$) which satisfies the separable differential equation

$$\frac{dy}{dx} = \frac{6+16x}{xy^2}; x > 0$$

with the initial condition: $y(1) = 3$

$y =$ _____

(function of x only)

15.(1 pt) Find the solution of the differential equation

$$(\ln(y))^4 \frac{dy}{dx} = x^4 y$$

which satisfies the initial condition $y(1) = e^2$

$y =$ _____

16.(1 pt) A. Solve the following initial value problem:

$$(t^2 - 16t + 15) \frac{dy}{dt} = y$$

with $y(8) = 1$. (Find y as a function of t .)

$y =$ _____

B. On what interval is the solution valid?

Answer: It is valid for _____ $< t <$ _____ .

C. Find the limit of the solution as t approaches the left end of the interval.

(Your answer should be a number or the word "infinite".)

Answer C: _____

D. Similar to C, but for the right end.

Answer D: _____

17.(1 pt) The differential equation

$$\frac{dy}{dx} = \cos(x) \frac{(y^2 + 5y + 6)}{(3y + 8)}$$

has an implicit general solution of the form $F(x, y) = K$.

In fact, because the differential equation is separable, we can define the solution curve implicitly by a function in the form

$$F(x, y) = G(x) + H(y) = K$$

Find such a solution and then give the related functions requested.

$$F(x, y) = G(x) + H(y) =$$

18.(1 pt) The differential equation

$$36 \frac{dy}{dx} = (25 - x^2)^{-1/2} \exp(-9y)$$

has an implicit general solution of the form $F(x,y) = K$.

In fact, because the differential equation is separable, we can define the solution curve implicitly by a function in the form $F(x,y) = G(x) + H(y) = K$

Find such a solution and then give the related functions requested.

$$F(x,y) = G(x) + H(y) =$$

19.(1 pt) The differential equation

$$\frac{dy}{dx} = \frac{18}{(y^{1/3} + 9x^2y^{1/3})}$$

has an implicit general solution of the form $F(x,y) = K$.

In fact, because the differential equation is separable, we can define the solution curve implicitly by a function in the form $F(x,y) = G(x) + H(y) = K$

Find such a solution and then give the related functions requested.

$$F(x,y) = G(x) + H(y) =$$

20.(1 pt) The differential equation

$$(5 + 2 \cos(x)) \frac{dy}{dx} = \sin(x) \cos(y)$$

has an implicit general solution of the form $F(x,y) = K$.

In fact, because the differential equation is separable, we can define the solution curve implicitly by a function in the form $F(x,y) = G(x) + H(y) = K$

Find such a solution and then give the related functions requested.

$$F(x,y) = G(x) + H(y) =$$

21.(1 pt) A. Find y in terms of x if

$$\frac{dy}{dx} = x^6 y^{-3}$$

and $y(0) = 9$.

$y(x) =$ _____

B. For what x -interval is the solution defined?

(Your answers should be numbers or plus or minus infinity.

For plus infinity enter "PINF" ; for minus infinity enter "MINF".)

The solution is defined on the interval:

_____ $< x <$ _____

22.(1 pt) The differential equation

$$\frac{dy}{dx} = \frac{(4x+4)}{(12y^2+10y+6)}$$

has an implicit general solution of the form $F(x,y) = K$.

In fact, because the differential equation is separable, we can define the solution curve implicitly by a function in the form $F(x,y) = G(x) + H(y) = K$

Find such a solution and then give the related functions requested.

$$F(x,y) = G(x) + H(y) =$$

23.(1 pt) The differential equation

$$\exp(y) \frac{dy}{dx} = \frac{(14x+3)}{(0 \sin(y) + 10 \cos(y))}$$

has an implicit general solution of the form $F(x,y) = K$.

In fact, because the differential equation is separable, we can define the solution curve implicitly by a function in the form $F(x,y) = G(x) + H(y) = K$

Find such a solution and then give the related functions requested.

$$F(x,y) = G(x) + H(y) =$$

24.(1 pt) A. Solve the following initial value problem:

$$\cos(t)^2 \frac{dy}{dt} = 1$$

with $y(16) = \tan(16)$.

(Find y as a function of t .)

$y =$ _____

B. On what interval is the solution valid?

(Your answer should involve pi.)

Answer: It is valid for _____ $< t <$ _____ .

C. Find the limit of the solution as t approaches the left end of the interval.

(Your answer should be a number or "PINF" or "MINF".

"PINF" stands for plus infinity and "MINF" stands for minus infinity.)

Answer C: _____

D. Similar to C, but for the right end.

Answer D: _____

25.(1 pt) The differential equation

$$\frac{dy}{dx} = (30 + 36x + 40y + 48xy)$$

has an implicit general solution of the form $F(x,y) = K$.

In fact, because the differential equation is separable, we can define the solution curve implicitly by a function in the form $F(x,y) = G(x) + H(y) = K$

Find such a solution and then give the related functions requested.

$$F(x,y) = G(x) + H(y) =$$
