

1.(1 pt) If the tangent line to $y = f(x)$ at $(4, -2)$ passes through the point $(8, -3)$, find

- A. $f(4) =$ _____
 B. $f'(4) =$ _____

2.(1 pt) The point $P(2, 11)$ lies on the curve $y = x^2 + x + 5$. If Q is the point $(x, x^2 + x + 5)$, find the slope of the secant line PQ for the following values of x .

- If $x = 2.1$, the slope of PQ is: _____
 and if $x = 2.01$, the slope of PQ is: _____
 and if $x = 1.9$, the slope of PQ is: _____
 and if $x = 1.99$, the slope of PQ is: _____
 Based on the above results, guess the slope of the tangent line to the curve at $P(2, 11)$. _____

3.(1 pt) The point $P(16, 8)$ lies on the curve $y = \sqrt{x} + 4$. If Q is the point $(x, \sqrt{x} + 4)$, find the slope of the secant line PQ for the following values of x .

- If $x = 16.1$, the slope of PQ is: _____
 and if $x = 16.01$, the slope of PQ is: _____
 and if $x = 15.9$, the slope of PQ is: _____
 and if $x = 15.99$, the slope of PQ is: _____
 Based on the above results, guess the slope of the tangent line to the curve at $P(16, 8)$. _____

4.(1 pt) The point $P(0.25, 8)$ lies on the curve $y = 2/x$. If Q is the point $(x, 2/x)$, find the slope of the secant line PQ for the following values of x .

- If $x = 0.35$, the slope of PQ is: _____
 and if $x = 0.26$, the slope of PQ is: _____
 and if $x = 0.15$, the slope of PQ is: _____
 and if $x = 0.24$, the slope of PQ is: _____
 Based on the above results, guess the slope of the tangent line to the curve at $P(0.25, 8)$. _____

5.(1 pt) If a ball is thrown straight up into the air with an initial velocity of 45 ft/s, its height in feet after t second is given by $y = 45t - 16t^2$. Find the average velocity for the time period beginning when $t = 2$ and lasting

- (i) 0.5 seconds _____
 (ii) 0.1 seconds _____
 (iii) 0.01 seconds _____

Finally based on the above results, guess what the instantaneous velocity of the ball is when $t = 2$. _____

6.(1 pt) A ball is thrown into the air by a baby alien on a planet in the system of Alpha Centauri with a velocity of 25 ft/s. Its height in feet after t seconds is given by $y = 25t - 12t^2$.

A. Find the average velocity for the time period beginning when $t=1$ and lasting

- .01 s: _____
 .005 s: _____

- .002 s: _____
 .001 s: _____

NOTE: For the above answers, you may have to enter 6 or 7 significant digits if you are using a calculator.

B. Estimate the instantaneous velocity when $t=1$. _____

7.(1 pt) The experimental data in the table below define y as a function of x .

| | | | | | | |
|---|---|-----|-----|-----|-----|-----|
| x | 0 | 1 | 2 | 3 | 4 | 5 |
| y | 2 | 0.7 | 0.4 | 0.6 | 1.2 | 2.2 |

A. Let P be the point $(4, 1.2)$. Find the slopes of the secant lines PQ when Q is the point of the graph with x coordinate x_1 .

| | | | | | |
|-------|---|---|---|---|---|
| x_1 | 0 | 1 | 2 | 3 | 5 |
| slope | — | — | — | — | — |

B. Draw the graph of the function for yourself and estimate the slope of the tangent line at P . _____

8.(1 pt) Below is an "oracle" function. An oracle function is a function presented interactively. When you type in an t value, and press the $-f->$ button and the value $f(t)$ appears in the right hand window. There are three lines, so you can easily calculate three different values of the function at one time.

The function $f(t)$ represents the height in feet of a ball thrown into the air, t seconds after it has been thrown.

Calculate the velocity 0.8 seconds after the ball has been thrown.

The velocity at 0.8 = _____ You can use a **calculator**

| | | |
|---------|---|----------------|
| t | → | f(t) |
| Enter t | → | result: $f(t)$ |
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| Enter t | → | result: $f(t)$ |

Remember this technique for finding velocities. Later we will use the same method to find the derivative of functions such as $f(t)$.

9.(1 pt) The position of a cat running from a dog down a dark alley is given by the values of the table.

| | | | | | | |
|------------|---|----|----|----|----|-----|
| t(seconds) | 0 | 1 | 2 | 3 | 4 | 5 |
| s(feet) | 0 | 15 | 22 | 73 | 96 | 109 |

A. Find the average velocity of the cat (ft/sec) for the time period beginning when $t=2$ and lasting

- a) 3 s _____
 b) 2 s _____
 c) 1 s _____

B. Draw the graph of the function for yourself and estimate the instantaneous velocity of the cat (ft/sec) when $t=2$. _____