

1.(1 pt)

Find the determinant of the matrix

$$A = \begin{bmatrix} -2 & -2 \\ 7 & -3 \end{bmatrix}$$

detA = \_\_\_\_\_

2.(1 pt)

Find the determinant of the matrix

$$B = \begin{bmatrix} 2 & -3 & 1 \\ 4 & 4 & 5 \\ -3 & 4 & -5 \end{bmatrix}$$

detB = \_\_\_\_\_

3.(1 pt)

Find the determinant of the matrix

$$C = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & -3 & -3 & 0 \\ 1 & 1 & -1 & -2 \\ 2 & 1 & -2 & 1 \end{bmatrix}$$

detC = \_\_\_\_\_

4.(1 pt) You'll need to use formatted text mode in order to do this problem: click the "formatted text" radio button at the bottom of the page and then click "submit answer".

If

$$A = \begin{pmatrix} -2 & -2 \\ 3 & 2 \end{pmatrix}$$

Then

$$\det(A) = \underline{\hspace{1cm}} \quad \text{and} \quad A^{-1} = \begin{pmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{pmatrix}$$

5.(1 pt) You'll need to use formatted text mode in order to do this problem: click the "formatted text" radio button at the bottom of the page and then click "submit answer".

If

$$A = \begin{pmatrix} 0 & 2 \\ 1 & -4 \end{pmatrix}$$

Then

$$\det(A) = \underline{\hspace{1cm}} \quad \text{and} \quad A^{-1} = \begin{pmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{pmatrix}$$

6.(1 pt)

Find the area of the parallelogram with vertices at (5, -3), (16, -12), (11, 8), and (22, -1).

Area = \_\_\_\_\_

7.(1 pt) Find the volume of the parallelepiped with one vertex at (0, 2, -1), and adjacent vertices at (-6, -5, -1), (7, 8, 6), and (7, 5, -3).

Area = \_\_\_\_\_

8.(1 pt)

Find  $k$  such that the matrix

$$M = \begin{bmatrix} -3 & 5 & -1 \\ -6 & 6 & -6 \\ 1+k & -1 & 5 \end{bmatrix}$$

is singular.

$k =$  \_\_\_\_\_

9.(1 pt)

If  $A$  and  $B$  are  $4 \times 4$  matrices,  $\det(A) = 2$ , and  $\det(B) = 4$ , then

$\det(AB) =$  \_\_\_\_\_

$\det(-2A) =$  \_\_\_\_\_

$\det(B^{-1}) =$  \_\_\_\_\_

$\det(B^3) =$  \_\_\_\_\_

10.(1 pt)

Consider the following general matrix equation:

$$\begin{pmatrix} a_1 \\ a_2 \end{pmatrix} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \end{pmatrix}$$

which can also be abbreviated as:

$$A = MX$$

By definition, the determinant of  $M$  is given by

$$\det(M) = m_{11}m_{22} - m_{12}m_{21}$$

The following questions are about the relationship between the determinant of  $M$  and the ability to solve the equation above for  $A$  in terms of  $X$  or for  $X$  in terms of  $A$ .

Check the boxes which make the statement correct:

**If the  $\det(M) \neq 0$  then**

- A. given any  $A$  there is one and only one  $X$  which will satisfy the equation.
- B. some values of  $X$  will have more than one value of  $A$  which satisfy the equation.
- C. given any  $X$  there is one and only one  $A$  which will satisfy the equation.
- D. some values of  $A$  will have no values of  $X$  which will satisfy the equation.
- E. some values of  $X$  will have no values of  $A$  which satisfy the equation.
- F. some values of  $A$  (such as  $A = 0$ ) will allow more than one  $X$  to satisfy the equation.

Check the boxes which make the statement correct:

**If the  $\det(M) = 0$  then**

- A. there is no value of  $X$  which satisfies the equation when  $A = 0$ .
- B. some values of  $A$  (such as  $A = 0$ ) will allow more than one  $X$  to satisfy the equation.
- C. given any  $A$  there is one and only one  $X$  which will satisfy the equation.

- D. given any  $X$  there is one and only one  $A$  which will satisfy the equation.
- E. some values of  $A$  will have no values of  $X$  which will satisfy the equation.

**Check the conditions that guarantee that  $\det(M) = 0$ :**

- A. Given any  $A$  there is one and only one  $X$  which will satisfy the equation.

- B. There is some value of  $A$  for which no value of  $X$  satisfies the equation.
- C. When  $A = 0$  there is more than one  $X$  which satisfies the equation.
- D. Given any  $X$  there is one and only one  $A$  which will satisfy the equation.