

1.(1 pt) Evaluate the following expressions.

- (a)  $\log_6 6^{11} =$  \_\_\_\_\_
- (b)  $\log_3 27 =$  \_\_\_\_\_
- (c)  $\log_5 125 =$  \_\_\_\_\_
- (d)  $\log_2 2^5 =$  \_\_\_\_\_

2.(1 pt) Evaluate the following expressions.

- (a)  $\log_2 \left(\frac{1}{16}\right) =$  \_\_\_\_\_
- (b)  $\log_2 1 =$  \_\_\_\_\_
- (c)  $\log_4 \sqrt{1024} =$  \_\_\_\_\_
- (d)  $5^{\log_5 9} =$  \_\_\_\_\_

3.(1 pt) Evaluate the following expressions.

- $\log_5 0.0016 =$  \_\_\_\_\_
- $\log_{10} 0.001 =$  \_\_\_\_\_
- $\log_{1024} \sqrt{4} =$  \_\_\_\_\_
- $\log_4 8 =$  \_\_\_\_\_

4.(1 pt) Evaluate the following expressions.

- (a)  $\ln e^{-3} =$  \_\_\_\_\_
- (b)  $e^{\ln 6} =$  \_\_\_\_\_
- (c)  $e^{\ln \sqrt{4}} =$  \_\_\_\_\_
- (d)  $\ln(1/e^3) =$  \_\_\_\_\_

5.(1 pt)

- (a) If  $\log_3 x = 3$ , then  $x =$  \_\_\_\_\_
- (b) If  $\log_5 x = 2$ , then  $x =$  \_\_\_\_\_

6.(1 pt)

- (a) If  $\log_x 8 = 3$ , then  $x =$  \_\_\_\_\_
- (b) If  $\log_x 16 = 2$ , then  $x =$  \_\_\_\_\_

7.(1 pt)

- (a) If  $6^x = 32$ , then  $x =$  \_\_\_\_\_
- (b) If  $14^{-x} = 6$ , then  $x =$  \_\_\_\_\_

8.(1 pt) Solve the given equation for  $x$ .

$3^{x-2} = 5$   
 $x =$  \_\_\_\_\_

9.(1 pt) Solve the given equation for  $x$ .

$5^{4x-4} = 38$   
 $x =$  \_\_\_\_\_

10.(1 pt)

If  $\ln(4x + 6) = 3$ , then  $x =$  \_\_\_\_\_

11.(1 pt) If  $e^{3x} = 26$ , then  $x =$  \_\_\_\_\_

12.(1 pt) Match the statements defined below with the letters labeling their equivalent expressions.

- 1.  $\ln(y^x)$
- 2.  $\ln(xy)$
- 3.  $\ln \frac{x}{y}$
- 4.  $\ln(x^y)$
- A.  $x \ln y$
- B.  $\ln x + \ln y$
- C.  $y \ln x$
- D.  $\ln x - \ln y$

13.(1 pt) Enter a T or an F in each answer space below to indicate whether the corresponding statement is true or false.

You must get all of the answers correct to receive credit.

- 1.  $(\ln a)^b = b \ln a$
- 2.  $\frac{\ln x}{\ln y} = \ln x - \ln y$
- 3.  $\log_a b = \log_b a$
- 4.  $\ln(x - y) = \ln x - \ln y$

14.(1 pt)

$$\ln(r^5 s^6 \sqrt[10]{r^2 s^3})$$

is equal to

$$A \ln r + B \ln s$$

where  $A =$  \_\_\_\_\_ and where  $B =$  \_\_\_\_\_

15.(1 pt) Evaluate the following expressions.

- (a)  $e^{5 \ln 4} =$  \_\_\_\_\_
- (b)  $10^{4 \log_{10} 5} =$  \_\_\_\_\_
- (c)  $\log_2 8^9 =$  \_\_\_\_\_

[NOTE: Your answers cannot be algebraic expressions. ]

16.(1 pt) If  $\ln x + \ln(x - 7) = \ln 6x$ , then  $x =$  \_\_\_\_\_

17.(1 pt) Solve the given equation for  $x$ .

$\log_{10} x + \log_{10}(x + 48) = 2$   
 $x =$  \_\_\_\_\_

18.(1 pt) Solve the given equation for  $x$ .

$7^{x/5} = 3$   
 $x =$  \_\_\_\_\_

19.(1 pt) Solve the given equation for  $x$ .

$\left(\frac{1}{5}\right)^x = 10$   
 $x =$  \_\_\_\_\_

20.(1 pt) Rewrite the expression in terms of  $\ln$

$\log_7 11 =$  \_\_\_\_\_

21.(1 pt) Rewrite the expression in terms of  $\ln$

$\log_{12} 8 =$  \_\_\_\_\_

22.(1 pt) The equation  $x^2 * 7^x - 7x * 7^x = 0$  has two roots. The smaller root is \_\_\_\_\_ and the bigger root is \_\_\_\_\_

23.(1 pt) The equation  $4x^6 e^{-9x} - 2x^7 e^{-9x} = 0$  has two roots. The smaller root is \_\_\_\_\_ and the bigger root is \_\_\_\_\_

24.(1 pt) The equation  $e^{2x} - 9e^x + 20 = 0$  has two solutions. The smaller one is: \_\_\_\_\_ and the larger one is: \_\_\_\_\_

25.(1 pt) If  $e^{2x} - 1e^x = +20$ , then  $x =$  \_\_\_\_\_

26.(1 pt) For each of the following, find the base  $b$  if the graph of  $y = b^x$  contains the given point.

- (3, 8)  $b =$  \_\_\_\_\_
- (2, 16)  $b =$  \_\_\_\_\_
- (0.5, 2)  $b =$  \_\_\_\_\_
- (0.5, 1.73205080756888)  $b =$  \_\_\_\_\_
- (4, 1)  $b =$  \_\_\_\_\_

$$(3, 64) b = \underline{\hspace{2cm}}$$

$$(3, 1) b = \underline{\hspace{2cm}}$$

$$(-4, 0.0625) b = \underline{\hspace{2cm}}$$

$$(3, 125) b = \underline{\hspace{2cm}}$$

$$(1, 1) b = \underline{\hspace{2cm}}$$

**27.**(1 pt) Determine the smallest integer  $x$  that satisfies the given inequality.

$$9\sqrt{2x} > 26$$

$$x > \underline{\hspace{2cm}}$$

$$x\sqrt{4} > 113$$

$$x > \underline{\hspace{2cm}}$$

$$3.8\sqrt{3x} > 31$$

$$x > \underline{\hspace{2cm}}$$

$$x\sqrt{\frac{9}{4}} > 31$$

$$x > \underline{\hspace{2cm}}$$

**28.**(1 pt) Starting with the graph of  $f(x) = 8^x$ , write the equation of the graph that results from

(a) shifting  $f(x)$  4 units upward.  $y = \underline{\hspace{2cm}}$

(b) shifting  $f(x)$  6 units to the right.  $y = \underline{\hspace{2cm}}$

(c) reflecting  $f(x)$  about the  $x$ -axis.  $y = \underline{\hspace{2cm}}$

(d) reflecting  $f(x)$  about the line  $x = 3$ .  $y = \underline{\hspace{2cm}}$