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1.(1 pt) Find the length of the given curve:

$$\mathbf{r}(t) = (3t, 5 \sin t, 5 \cos t)$$

where  $-3 \leq t \leq 5$ .

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2.(1 pt) Starting from the point  $(-5, -4, -4)$  reparametrize the curve

$$\mathbf{r}(t) = (-5 - 2t)\mathbf{i} + (-4 + 2t)\mathbf{j} + (-4 - 1t)\mathbf{k}$$

in terms of arclength.

$$\mathbf{r}(t(s)) = \underline{\hspace{2cm}} \mathbf{i} + \underline{\hspace{2cm}} \mathbf{j} + \underline{\hspace{2cm}} \mathbf{k}$$


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3.(1 pt) If  $\mathbf{r}(t) = \cos(-1t)\mathbf{i} + \sin(-1t)\mathbf{j} - 6t\mathbf{k}$ , compute:

A. The velocity vector  $\mathbf{v}(t) = \underline{\hspace{1cm}} \mathbf{i} + \underline{\hspace{1cm}} \mathbf{j} + \underline{\hspace{1cm}} \mathbf{k}$

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B. The acceleration vector  $\mathbf{a}(t) = \underline{\hspace{1cm}} \mathbf{i} + \underline{\hspace{1cm}} \mathbf{j} + \underline{\hspace{1cm}} \mathbf{k}$   
 Note: the coefficients in your answers must be entered in the form of expressions in the variable  $t$ ; e.g. " $5 \cos(2t)$ "

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4.(1 pt) Consider the helix  $\mathbf{r}(t) = (\cos(1t), \sin(1t), 3t)$ . Compute, at  $t = \frac{\pi}{6}$ :

A. The unit tangent vector  $\mathbf{T} = (\underline{\hspace{1cm}}, \underline{\hspace{1cm}}, \underline{\hspace{1cm}})$

B. The unit normal vector  $\mathbf{N} = (\underline{\hspace{1cm}}, \underline{\hspace{1cm}}, \underline{\hspace{1cm}})$

C. The unit binormal vector  $\mathbf{B} = (\underline{\hspace{1cm}}, \underline{\hspace{1cm}}, \underline{\hspace{1cm}})$

D. The curvature  $\kappa = \underline{\hspace{2cm}}$

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5.(1 pt) Find the curvature  $\kappa(t)$  of the curve  $\mathbf{r}(t) = (-5 \sin t)\mathbf{i} + (-5 \sin t)\mathbf{j} + (4 \cos t)\mathbf{k}$

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6.(1 pt) Find the curvature of  $y = \sin(2x)$  at  $x = \frac{\pi}{4}$ .

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