

## PROBLEM SET 8

[J]=Jacobson. Problems 7-10 are based on stuff we will discuss on Wednesday (and maybe Friday).

- (1) [J] p. 349 #4
- (2) [J] p. 353 #1
- (3) [J] p. 396 #1
- (4) [J] p. 397 #6
- (5) [J] p. 397 #7
- (6) Finish the proof of the extension-of-basis lemma from the beginning of Monday's class: if  $(V, B)$  is a symplectic vector space (that is,  $B$  is assumed non-degenerate and alternating), then a linearly independent, isotropic subset  $\{u_1, \dots, u_k\} \subset V$  may be extended to a symplectic basis of  $V$ . [Notes: in the proof,  $V$  was called  $U''$  and the span of the  $u_i$  was  $R$ . Also, a set  $S \subset U$  is isotropic if  $B(S, S) = \{0\}$ .]
- (7) [J] p. 361 #1
- (8) [J] p. 361 #3
- (9) [J] p. 361 #4
- (10) [J] p. 404 #1