## Homework 2

Math 109 / Music 109A, Fall 2022

Due Monday, October 3.

1. In ${ }_{2}^{3}$ time, give the duration in beats for:
(a) an eighth note
(b) a dotted half note
(c) a quarter note with four dots
2. In ${ }_{8}^{9}$ time, taken as a compound time signature, give the duration in beats for:
(a) a quarter note
(b) an eighth note
(c) an eighth note tied to a thirty-second note
3. Prove the equation:

$$
1+r+r^{2}+\cdots+r^{m}=\frac{1-r^{m+1}}{1-r}
$$

for any integer $m \geq 0$ and any real number $r \neq 1$. Hint: Consider the product $(1-r)\left(1+r+r^{2}+\cdots+r^{m}\right)$. Explain how this relates to the durations of dotted notes.
4. Notate and name the following tuplets:
(a) that which divides the whole note into 3 equal notes
(b) that which divides the half note into 7 equal notes
(c) that which divides the quarter note into 13 equal notes
5. Notate and give the total duration, in ${ }_{4}^{4}$ time, of:
(a) a sixteenth note quintuplet
(b) an eighth note triplet
(c) a sixteenth note 17-tuplet
6. Complete these measures with a single durational note:
(a)

(b)

(c)

7. Complete the following example three ways with a measure having the same rhythm,

employing, respectively:
(a) diatonic transposition up three scale tones
(b) diatonic transposition down one scale tone
(c) chromatic transposition one step (two semitones)

Which of of these, if any, represent both diatonic and chromatic transposition?
8. For the refrain of the song Carolina In the Morning,, give the form (e.g., $\mathrm{ABA}^{\prime} \mathrm{C}$ or ABA ) by dividing the chorus of the song (which begins on page 3) into segments consisting of eight measures.

For the same chorus, locate transformations such as translation (melodic and/or rhythmic) and transposition (diatonic and/or chromatic), other than those that are dictated by the global form determined above.

A pdf copy of song is posted on the course web page under Handouts. You may reference your discussion by numbering the measures, letting measure 1 be the first measure of the chorus.
9. The tonic triad of a mode is the chord consisting of its scale tones $\hat{1}, \hat{3}$, and $\hat{5}$. For each of the seven modes name the chord type of the tonic triad.
10. Consider the equivalence relation $\equiv$ on $\mathbb{Z}$ defined by $k \equiv \ell$ if and only if $12 \mid(k-\ell)$. Now consider the equivalence $\sim$ relation on $\mathbb{Z}$ defined by $k \sim \ell$ if and only if the musical intervals $k$ semitones and $\ell$ semitones differ by a multi-octave (i.e., give the same modular interval). Explain why these are the same equivalence relation.

